

# A Genomic Approach to Study the Properties and Correlations of MAX Phases

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*2014 NETL Crosscutting Research Review Meeting  
Sheraton Station Square Hotel, Pittsburgh, PA  
May 19-23, 2014*

**Project:** DOE- NETL grant DE-FE00005865  
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# I. Outline

- I. Introduction to MAX phases
- II. **Genomic** approach to study MAX phases
- III. Computational methods
- IV. **Analysis of results**
- V. Summary and Conclusions
- VI. **Future work**

# I. Introduction to MAX Phases

**Why MAX phases?** A novel class of intermetallic compounds with unique properties serving as a **model system** for **Genomic data base**.

**What is MAX?** Layered Ternary Transition Metal Carbides and Nitrides.

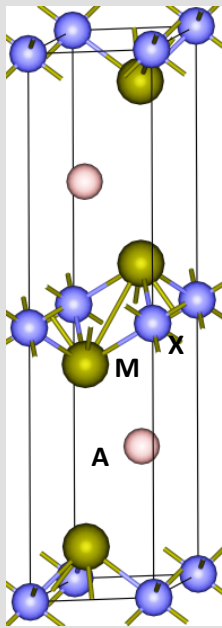
**Formula:**  $M_{n+1}AX_n$  where **M** — Early Transition Metal; **A** — A-group element; **X** — Carbide or Nitride,  $n = 1, 2, 3, 4$ . ( $n > 4$  also possible)

Most MAX phases are 211 or 312 compounds; 413 and 514 are very rare.

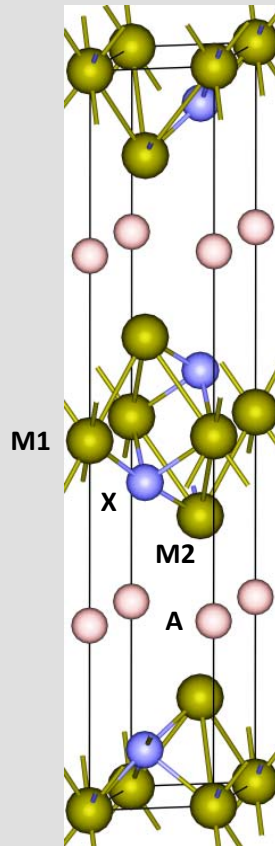
The periodic table highlights the components of MAX phases. The legend indicates: **M** (red) is an early transition metal; **A** (blue) is a group A element; and **X** (black) is Carbon and/or Nitrogen. The highlighted elements are: Sc, Ti, V, Cr, Zr, Nb, Mo, Hf, Ta, Al, Si, P, S, Ga, Ge, As, In, Sn, Sb, Te, I, Xe, Cd, Hg, Tl, Pb, Bi, Po, At, Rn.

| IA | IIA |    |     |     |     |     |     |     |    |    | IIIA      | IVA       | VA        | VIA      | VII | VIIIA |    |
|----|-----|----|-----|-----|-----|-----|-----|-----|----|----|-----------|-----------|-----------|----------|-----|-------|----|
|    |     |    |     |     |     |     |     |     |    |    |           |           |           |          |     | He    |    |
| Li | Be  |    |     |     |     |     |     |     |    |    | B         | <b>C</b>  | <b>N</b>  | O        | F   | Ne    |    |
| Na | Mg  |    |     |     |     |     |     |     |    |    | <b>Al</b> | <b>Si</b> | <b>P</b>  | <b>S</b> | Cl  | Ar    |    |
| K  | Ca  | Sc | Ti  | V   | Cr  | Mn  | Fe  | Co  | Ni | Cu | Zn        | Ga        | Ge        | As       | Se  | Br    | Kr |
| Rb | Sr  | Y  | Zr  | Nb  | Mo  | Tc  | Ru  | Rh  | Pd | Ag | <b>Cd</b> | In        | Sn        | Sb       | Te  | I     | Xe |
| Cs | Ba  | Lu | Hf  | Ta  | W   | Re  | Os  | Ir  | Pt | Au | Hg        | <b>Tl</b> | <b>Pb</b> | Bi       | Po  | At    | Rn |
| Fr | Ra  | Lr | Unq | Unp | Unh | Uns | Uno | Une |    |    |           |           |           |          |     |       |    |

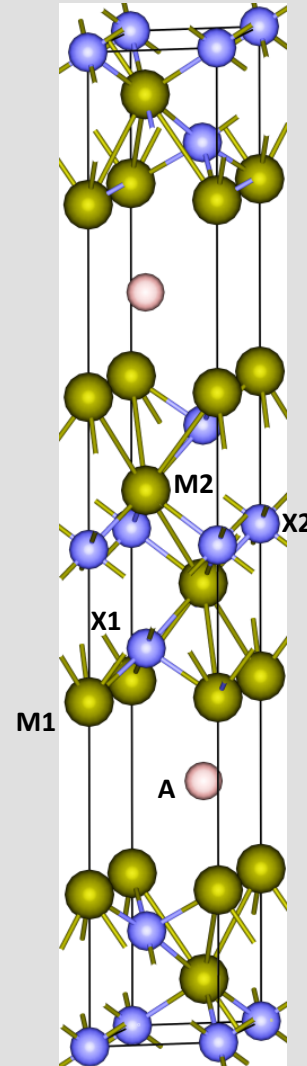
# Sketch of layered hexagonal crystal structure of 211, 312, 413, 514 MAX phases



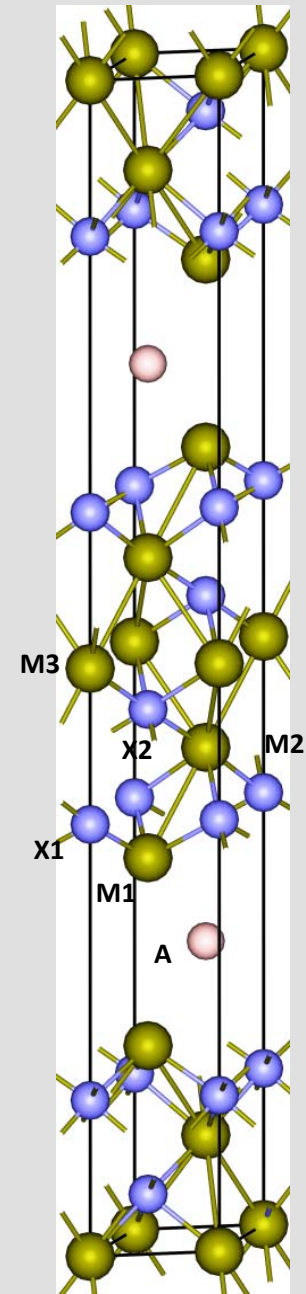
$M_2AX$



$M_3AX_2$



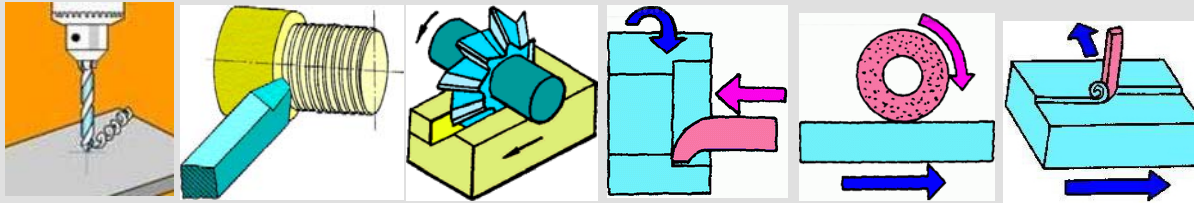
$M_4AX_3$



$M_5AX_4$

## Special properties of MAX phases

- ♠ **Like a Metal:** thermally and electrically conductive, thermal-shock resistant, machinable, and damage tolerant;



Images from the Internet

- ♠ **Like Ceramics:** light weight, stiff, refractory and oxidation resistant, not expensive.
- ♠ Mechanical properties of MAX phases are very complicated, depending on structure, composition and interatomic bonding.
- ♠ There are many real and projected applications for MAX phases.
- ♠ We focus on fundamental understanding and construction of the data base that can lead to these application.
- ♠ We explore its application to **fossil energy** technology.

## II. Genomic approach to mechanical properties

- ♠ There are many published papers on properties of MAX phases but data are scattered.
- ♠ An ambitious approach: get data for **All MAX phases**, properly screened and studied in detail => a **genomic approach**.
- ♠ Construction of a “complete” data base for All possible MAX phases for statistical data-mining and machine learning.
- ♠ Consider trends in the rows and columns of elements **M**, and **A**.
- ♠ Consider difference between **X** = C and **X** = N and trends in n.
- ♠ Consider correlations between **M**, **A**, **X**.
- ♠ Consider connections to electronic structures and bonding.
- ♠ Predict new stable MAX phases having outstanding properties.
- ♠ Identify the **genes** in MAX phases for targeted applications.
- ♠ Focus on fundamental understanding of MAX phases compounds.

### III. Computational methods (DFT-based calculations)

#### Mechanical properties calculations:

Use Vienna *Ab initio* Simulation Package (**VASP**) for relaxation, a stress- strain analysis under linear elastic theory to first obtain elastic coefficients  $C_{ij}$ . Apply RVH approximation for poly-crystals to obtain bulk modulus (K), Shear modulus (G), Young's modulus (E) and Poisson's ratio ( $\eta$ ), Pugh ratio G/K.

#### Electronic structure characterization:

Use first-principles orthogonalized linear combination of atomic orbitals (**OLCAO**) method for electronic structure calculation. OLCAO is a Density Functional Theory using LDA and atomic orbitals for basis expansion developed by us.

**Effective Charge  $Q^*$**  on each atom, **Bond Order values**  $\rho_{\alpha\beta}$  for each pair of atoms:

$$Q_{\alpha}^* = \sum_i \sum_{n,occ.} \sum_{j,\beta} C_{i\alpha}^{m*} C_{j\beta}^m \langle b_{i\alpha}(\vec{k}, \vec{r}) | b_{j\beta}(\vec{k}, \vec{r}) \rangle$$

$$\rho_{\alpha\beta} = \sum_{n,occ.} \sum_{j,\beta} C_{i\alpha}^{n*} C_{j\beta}^n \langle b_{i\alpha}(\vec{k}, \vec{r}) | b_{j\beta}(\vec{k}, \vec{r}) \rangle$$

We advocate that the **total bond order density** or **TBOD** (sum of all bonds in the crystal divided by volume) as the single most important parameter representing the electronic structures, the **gene**!



## Project started 1/1/2011. Papers published, accepted or submitted:

- ♠ Yuxiang Mo, Paul Rulis, **W.Y. Ching**, “Electronic Structure and Optical Conductivities of 20 MAX-Phase Compounds”, Phys. Rev. B86, 165122-1-10 (2012).
- ♠ A. Misra and **W.Y. Ching**. “*Ab initio* multi-axial tensile stress-strain-failure behavior of crystalline hydroxyapatite”. Scientific Research, #:1488 (2013).
- ♠ S. Aryal, M. C. Gao, L. Ouyang, and P. Rulis, **W. Y Ching**,”*Ab initio* studies of Mo-based alloys: mechanical, elastic and vibrational properties”, Intermetallics. 38, 116-125 (2013)
- ♠ **W.Y. Ching**, Yuxiang Mo, Sitaram Aryal and Paul Rulis, “Intrinsic mechanical properties of 20 MAX phase compounds”, J. Amer. Ceram. Soc. 1-6 (2013).
- ♠ C. C. Dharamawardhana, R. Sakidja and **W. Y. Ching**, “Temperature dependent mechanical properties of Mo-Si-B compounds via ab-initio molecular dynamics”, APL-Materials.1,012106 (2013).
- ♠ Liaoyuan Wang, Paul Rulis, **W. Y. Ching**, “Calculation of core-level excitation in some MAX phase compounds”, J. Appl. Phys. 114, 023708 (2013).
- ♠ Neng Li, C. C. Dharamawardhana, K.L. Yao and **W.Y. Ching**, ”Theoretical characterization on intrinsic ferromagnetic phase in naoscale laminated Cr<sub>2</sub>GeC”. Solid State Commun.,174 43–45 (2013).
- ♠ Neng Li, R. Sakidja and **W.Y. Ching**, “Oxidation of Cr<sub>2</sub>AlC (0001): “Insights from *ab initio* calculations”, JOM, Published on line (2013). DOI: 10.1007/s11837-013-0741-x.
- ♠ Yuxiang Mo, S. Aryal, Paul Rulis and **W.Y. Ching**, “Crystalline Structure and Elastic properties of MAX-like (Cr<sub>2</sub>Hf)<sub>2</sub>AlC“, J. Amer. Ceram. Soc. (accepted and in press).
- ♠ Neng Li, R. Sakidja and **W.Y. Ching**, “DFT Characterization on the Oxidation Processes of a Single O Atom and O<sub>2</sub> Molecule on the Cr<sub>2</sub>AlC (0001) Surface”, submitted to Appl. Surface Sci.
- ♠ S. Aryal, Ridwan Sakidja, M. Barsoum and **W.Y. Ching**, “**A Genomic Approach to the Stability, Elastic and Electronic Properties of the MAX Phases**”, Physica Status Solidi B. (in Press)





**Several more papers currently under preparation, expect to be published this year.**

- ♠ A. Hussain, R. Sakidja, and W-Y Ching, *Ab initio* Molecular Dynamics (AIMD) Study and Potential Development of Ti-Si-C Metallic System, to be submitted
- ♠ R. Sakidja and W-Y Ching, Ab Initio Molecular Dynamics (AIMD) Study on Phase Stability and Li Ion Mobility on 2-D MXenes (M = Group IVB – VIB, X = C/N), to be submitted.
- ♠ . C.C. Dharmawardhana, R. Sakidja, S. Aryal, W. Y. Ching, Computational design of thermal expansion in  $\text{Mo}_5\text{Si}_3$  - T1 alloyed phase, to be submitted.
  
- ♠ R. Sakidja, N. Li and W-Y Ching, Ab initio Molecular Dynamics (AIMD) Study on the Early Stage of Oxidation on  $\text{Cr}_2\text{AlC}$  and  $\text{Ti}_2\text{AlC}$  MAX Phases, in preparation
- ♠ R. Sakidja and A. Hussain and W-Y Ching, Development of Embedded Atom Model (EAM) and Angular Dependent Potential (ADP) for Ti-Al-C Ternary System, in preparation.
- ♠ C Dahkal, S. Aryal, R. Sakidja, and W. Y. Ching, In what way MAX nitrides differ from MAX carbides and why? in preparation.

## IV. Analysis of results MAX phases

### Phase I: Test calculations on 20 MAX phases. (first 2 years!)

- ♠ Select 20 MAX phases of different components and compositions.
- ♠ Calculate the electronic structure, bonding & optical conductivities of these 20 MAX phases. **(Done!)**

*Yuxiang Mo, Paul Rulis, W.Y. Ching, "Electronic Structure and Optical Conductivities of 20 MAX-Phase Compounds", Phys. Rev. B86, 165122-1-10 (2012).*

- ♠ Calculate the elastic and mechanical properties of the same 20 MAX phases. **(Done!)**

*W.Y. Ching, Yuxiang Mo, Sitaram Aryal and Paul Rulis, "Intrinsic mechanical properties of 20 MAX phase compounds", J. Amer. Ceram. Soc. 1-6 (2013) DOI:10.1111/jace.12376*

- ♠ **Phases II**, all MAX phases! (This presentation!)

# Elastic coefficients and mechanical properties of **20** MAX phases

| Crystals                                   | $C_{11}$     | $C_{12}$ | $C_{13}$ | $C_{33}$     | $C_{44}$ | $C_{66}$ | K     | G     | E     | $\eta$       | G/K=k       |
|--|--------------|----------|----------|--------------|----------|----------|-------|-------|-------|--------------|-------------|
| Ti <sub>3</sub> AlC <sub>2</sub>           | 355.8        | 81.4     | 75.3     | 293.4        | 120.3    | 137.2    | 162.5 | 126.7 | 301.7 | 0.191        | 0.78        |
| Ti <sub>3</sub> SiC <sub>2</sub>           | 369.6        | 96.2     | 107.6    | 358.3        | 155.0    | 136.7    | 191.1 | 141.3 | 340.0 | 0.204        | 0.74        |
| Ti <sub>3</sub> GeC <sub>2</sub>           | 362.0        | 97.2     | 97.7     | 332.0        | 137.3    | 132.4    | 182.2 | 132.2 | 319.3 | 0.208        | 0.73        |
| Ti <sub>2</sub> AlC                        | 301.9        | 68.0     | 63.0     | 267.9        | 105.1    | 117.0    | 139.7 | 110.5 | 262.3 | 0.187        | 0.79        |
| Ti <sub>2</sub> GaC                        | 300.8        | 79.2     | 63.8     | 246.5        | 92.4     | 110.8    | 139.3 | 101.4 | 244.9 | 0.207        | 0.73        |
| Ti <sub>2</sub> InC                        | 284.4        | 69.3     | 55.2     | 235.5        | 83.9     | 107.5    | 128.6 | 96.0  | 230.5 | 0.201        | 0.75        |
| Ti <sub>2</sub> SiC                        | 312.9        | 82.1     | 110.4    | 329.2        | 149.6    | 115.4    | 173.0 | 124.9 | 302.0 | 0.209        | 0.72        |
| Ti <sub>2</sub> GeC                        | 296.6        | 85.7     | 96.8     | 297.1        | 121.5    | 105.5    | 161.0 | 110.0 | 268.8 | 0.222        | 0.68        |
| Ti <sub>2</sub> SnC                        | 262.6        | 88.6     | 73.1     | 255.2        | 96.8     | 87.0     | 138.8 | 92.4  | 226.8 | 0.228        | 0.67        |
| <b>Ti<sub>2</sub>PC</b>                    | <b>256.8</b> | 144.8    | 155.0    | <b>339.5</b> | 166.3    | 56.0     | 191.8 | 93.1  | 240.4 | <b>0.291</b> | <b>0.49</b> |
| <b>Ti<sub>2</sub>AsC</b>                   | <b>212.9</b> | 180.4    | 123.7    | <b>289.5</b> | 146.3    | 16.2     | 150.7 | 57.2  | 152.3 | <b>0.332</b> | <b>0.38</b> |
| Ti <sub>2</sub> SC                         | 339.8        | 101.4    | 109.7    | 361.9        | 159.5    | 119.2    | 186.8 | 134.4 | 325.2 | 0.210        | 0.72        |
| Ti <sub>2</sub> AlN                        | 312.9        | 73.0     | 95.5     | 290.7        | 126.1    | 120.0    | 160.5 | 117.4 | 283.1 | 0.206        | 0.73        |
| V <sub>2</sub> AlC                         | 334.4        | 71.5     | 106.0    | 320.8        | 149.8    | 131.5    | 172.9 | 132.1 | 315.9 | 0.196        | 0.76        |
| Nb <sub>2</sub> AlC                        | 316.6        | 86.3     | 117.0    | 288.6        | 137.6    | 115.2    | 173.6 | 116.4 | 285.5 | 0.226        | 0.67        |
| Cr <sub>2</sub> AlC                        | 366.3        | 85.8     | 111.3    | 356.9        | 142.9    | 140.2    | 189.6 | 137.0 | 331.2 | 0.209        | 0.72        |
| Ta <sub>2</sub> AlC                        | 344.5        | 112.2    | 137.1    | 327.9        | 152.3    | 116.1    | 198.8 | 124.1 | 308.1 | 0.242        | 0.62        |
| $\alpha$ -Ta <sub>3</sub> AlC <sub>2</sub> | 453.6        | 130.5    | 135.6    | 388.4        | 175.0    | 161.5    | 232.8 | 161.1 | 392.8 | 0.219        | 0.69        |
| $\alpha$ -Ta <sub>4</sub> AlC <sub>3</sub> | 459.2        | 149.1    | 148.7    | 383.1        | 170.5    | 155.0    | 243.0 | 155.3 | 384.1 | 0.237        | 0.64        |
| Ta <sub>5</sub> AlC <sub>4</sub>           | 481.5        | 149.6    | 158.1    | 423.6        | 188.8    | 165.9    | 257.2 | 169.1 | 416.0 | 0.231        | 0.66        |

Anisotropic ratio  $C_{33}/C_{11}$  correlates with G/K. Note: **Ti<sub>2</sub>PC** and **Ti<sub>2</sub>AsC** are outliers.



## Electronic structure and bonding in the same **20** MAX phases

| MAX                 | $\Delta Q^*(M)$ | $\Delta Q^*(X)$ | $\Delta Q^*(A)$ | TBO    | BO(M-X) | BO(M-M) | BO(M-A) | BO(A-A) | $N(E_F)$ |
|---------------------|-----------------|-----------------|-----------------|--------|---------|---------|---------|---------|----------|
| Ti <sub>2</sub> AlC | -0.330          | -0.043          | 0.703           | 23.510 | 10.258  | 4.512   | 7.231   | 1.508   | 11.052   |
| Ti <sub>2</sub> GaC | -0.485          | 0.269           | 0.701           | 22.680 | 10.289  | 4.060   | 6.986   | 1.340   | 10.572   |
| Ti <sub>2</sub> InC | -0.424          | 0.148           | 0.700           | 22.750 | 10.238  | 4.396   | 6.482   | 1.636   | 9.260    |
| Ti <sub>2</sub> SiC | -0.393          | 0.097           | 0.688           | 22.820 | 10.344  | 3.583   | 8.153   | 0.742   | 12.921   |
| Ti <sub>2</sub> GeC | -0.509          | 0.324           | 0.694           | 21.750 | 10.337  | 3.541   | 7.111   | 0.758   | 14.720   |
| Ti <sub>2</sub> SnC | -0.381          | 0.069           | 0.693           | 22.320 | 10.294  | 3.926   | 7.110   | 0.993   | 15.084   |
| Ti <sub>2</sub> PC  | -0.454          | 0.210           | 0.699           | 22.740 | 10.366  | 2.802   | 9.571   | 0.000   | 21.762   |
| Ti <sub>2</sub> AsC | -0.505          | 0.316           | 0.695           | 21.360 | 10.382  | 2.893   | 8.086   | 0.000   | 19.697   |
| Ti <sub>2</sub> SC  | -0.447          | 0.189           | 0.705           | 21.340 | 10.380  | 2.944   | 8.018   | 0.000   | 7.301    |
| Ti <sub>2</sub> AlN | -0.295          | -0.087          | 0.679           | 22.150 | 8.702   | 4.646   | 7.217   | 1.585   | 15.502   |
| V <sub>2</sub> AlC  | -0.277          | -0.101          | 0.655           | 22.820 | 10.017  | 4.192   | 6.905   | 1.704   | 21.663   |
| Nb <sub>2</sub> AlC | -0.493          | 0.245           | 0.741           | 15.410 | 7.319   | 1.253   | 5.354   | 1.399   | 13.338   |
| Cr <sub>2</sub> AlC | -0.098          | -0.324          | 0.521           | 21.250 | 9.559   | 2.837   | 7.080   | 1.769   | 24.384   |
| Ta <sub>2</sub> AlC | -0.324          | -0.044          | 0.692           | 24.810 | 10.130  | 5.724   | 7.561   | 1.397   | 11.126   |

We now have such data Table for ALL MAX phases.

Data publically available: [Physica Status Solidi B. \(in Press\).](#)

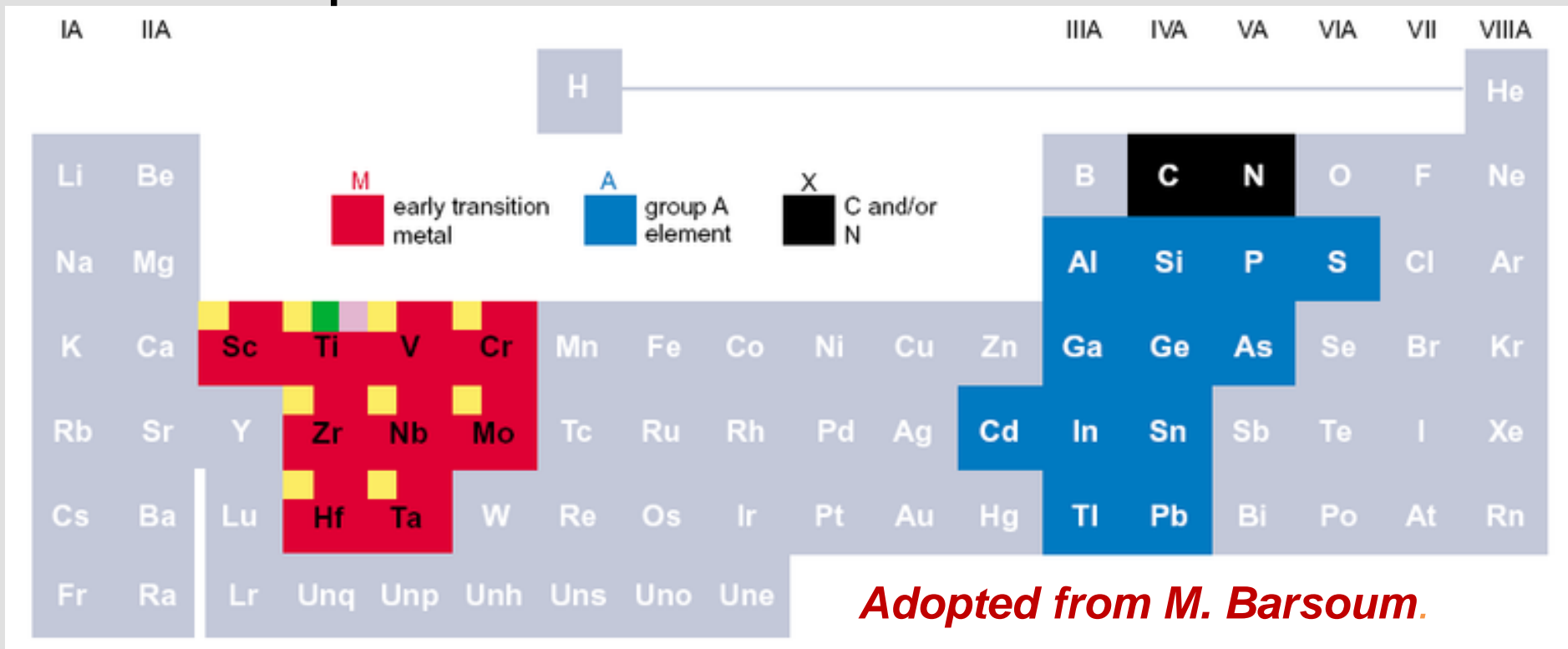
**M** (9): Sc (III<sub>A</sub>); Ti, Zr, Hf (IV<sub>A</sub>); V, Nb, Ta (V<sub>A</sub>); Cr, Mo (VI<sub>A</sub>).

**A** (11): Al, Ga, In, Tl (III<sub>B</sub>); Si, Ge, Sn, Pb (IV<sub>B</sub>); P, As (V<sub>B</sub>); S(VI<sub>B</sub>).

**X** (2): C (IV<sub>B</sub>) or N (V<sub>B</sub>).

n = 1, 211 phase; n = 2, 312 phase; n = 3, 413 phases; n = 4, 514 phase.

**Possible MAX phase considered: 9 x 11 x 2 x 4 = 792!**



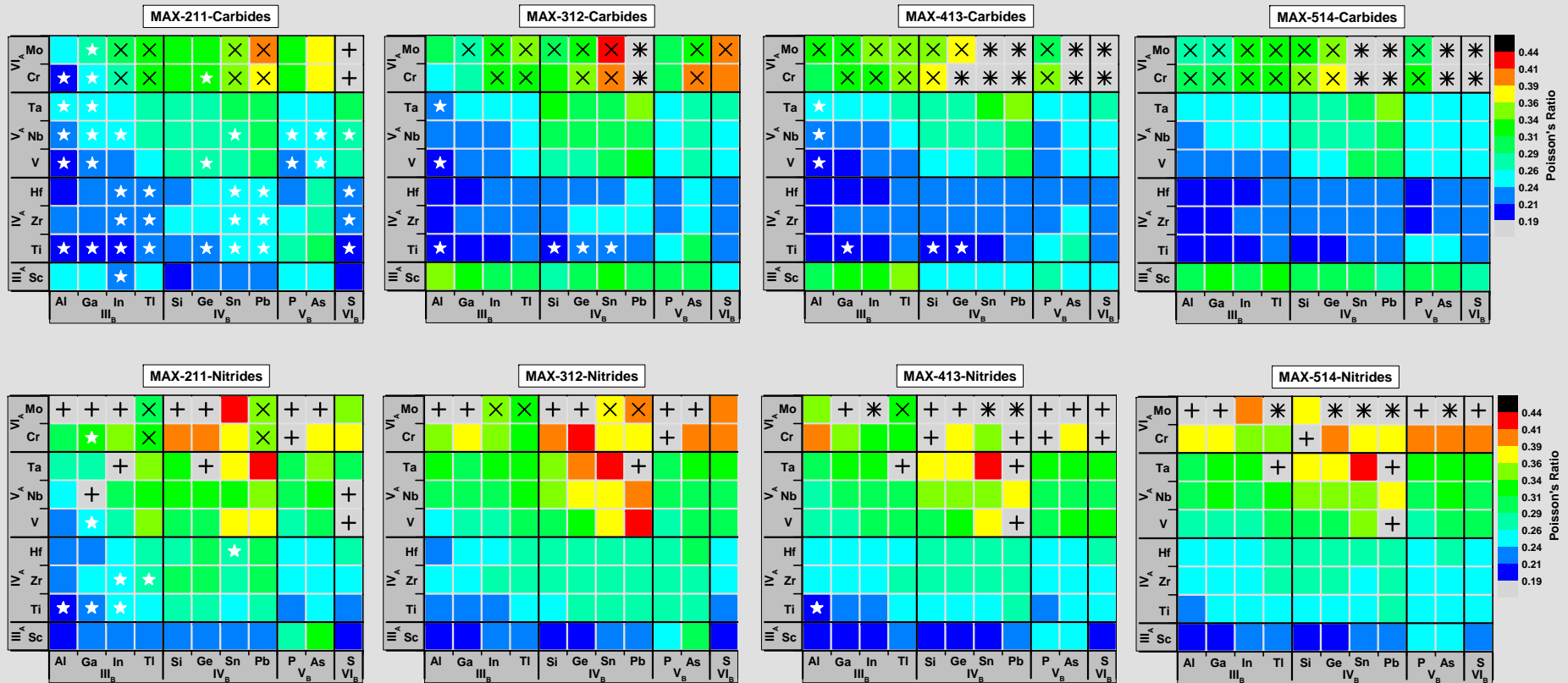
## **Phase II:** Expand to all 792 MAX phases. **(This presentation!)**

- ♠ Screen 792 MAX phases for mechanical (use Born Cauchy criterion) and thermodynamic stability (use heat of formation).
- ♠ Screening resulted in a large database of 665 viable MAX crystals.
- ♠ Find the **trends and correlations** in properties:
  - (1) Between elastic properties,
  - (2) Between electronic properties,
  - (3) Between mechanical and electronic structures.
- ♠ Only a few **selective results** on above properties and correlations are presented here due to time limitation.
- ♠ Use the database to test efficacy of **data-mining algorithm**.
- ♠ Predict stable **new phases** (outliers) with special properties.

**Warning!** Results presented below are very selective & highly condensed!

792 unscreened data in the form of Maps.

665 screened data in the form of scattered plots.



- ♠ Poisson's ratio ( $\eta$ ) maps for all MAX carbides (upper) and nitrides (lower) according to **M** (Y-axis) and **A** (X-axis) elements. Color in the box represents calculated  $\eta$  values.
- ♠ Stars in the box indicate => phases have been synthesized. '+' stands for elastic instability; 'x' indicates thermodynamic instability (HoF).
- ♠ All confirmed MAX phases (~60 of them) are stable. There are more stable ones unexplored.

G/K, the most representative value for the mechanical properties. Data for 665 MAX phases passed the screen are presented!

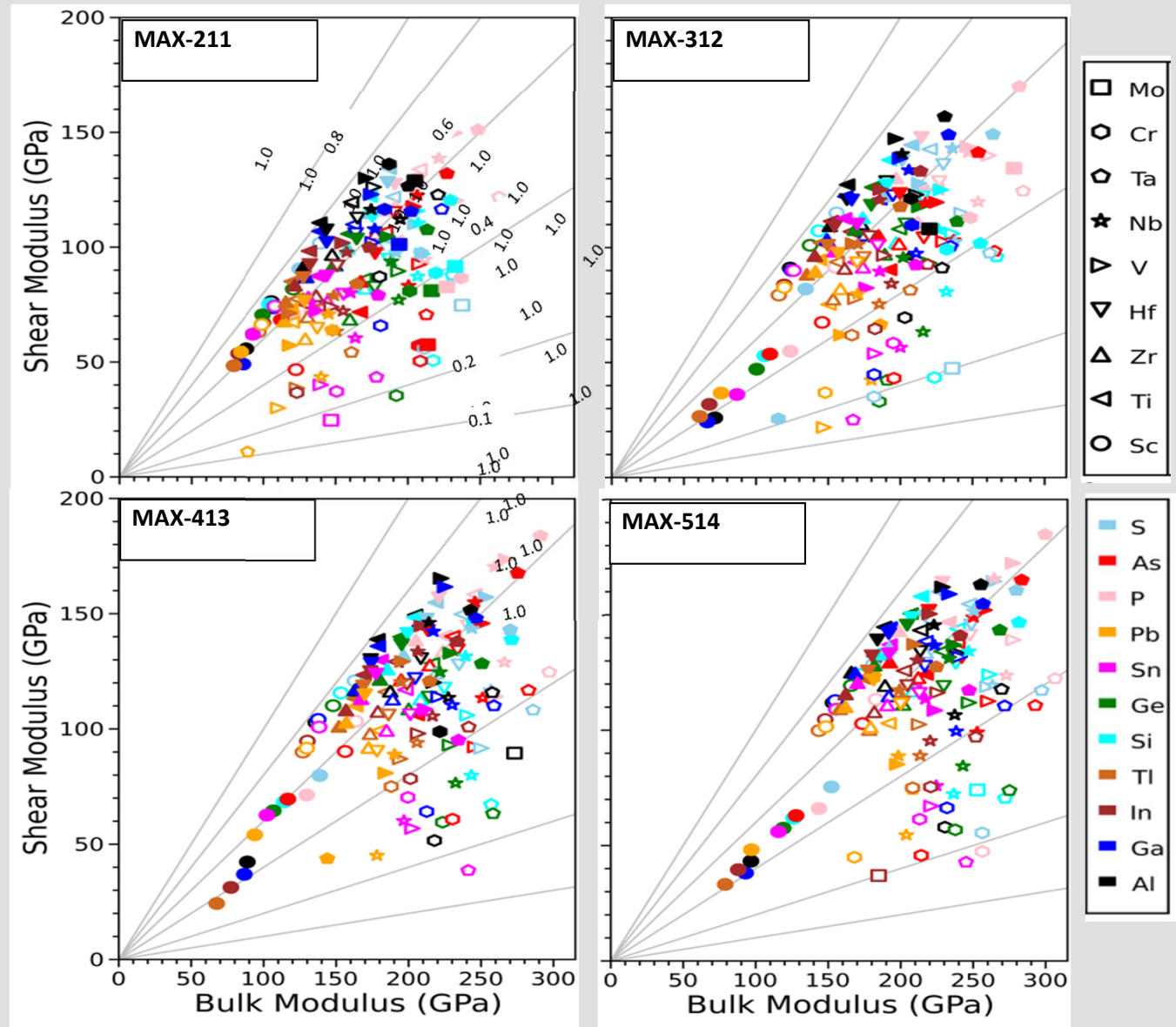
Comments:

♠ Very busy slide: Different shape for different **M**, different color for different **A**.

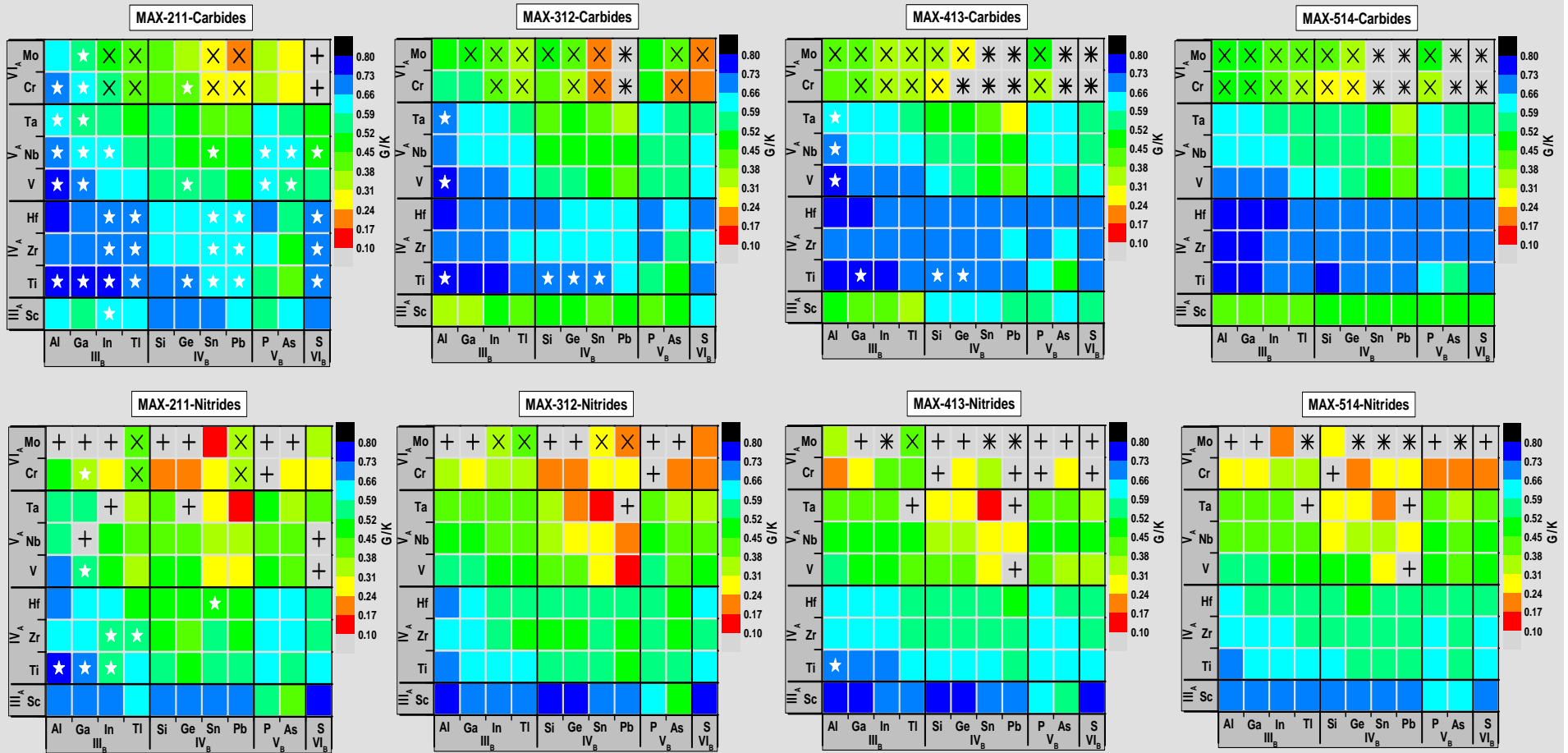
♠ All data for G and K plotted on a single figure.

♠ Slopes give G/K ratio for each crystal!

♠ G/K map in the next slide.



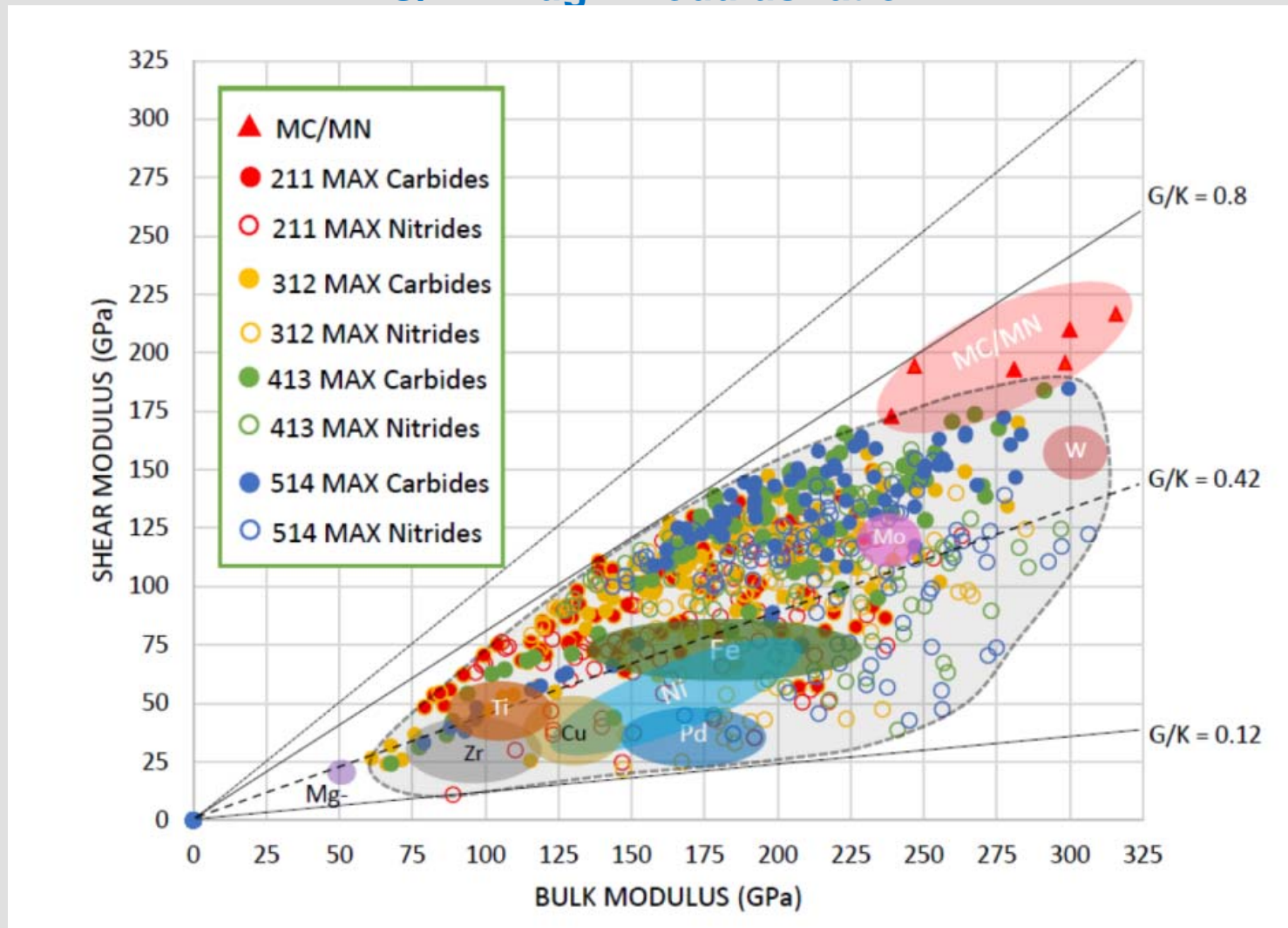




G/K maps for all MAX carbides (upper) and nitrides (lower) according to **M** (Y-axis) and **A** (X-axis) elements. Color in the box represents calculated G/K values. (This plot is **similar** to previous one for the Poisson's ratio.)

# Bulk modulus K vs. Shear modulus G plot for **all** MAX phases

$G/K =$  Pugh modulus ratio



MAX covers a wide range of  $G/K$  (0.8 – 0.18). Both ductile ( $G/K < 0.42$ ) and brittle ( $G/K > 0.42$ ).  
 Note the difference between nitrides and carbides.

# (1) Elastic Property Results:

Correlation plots of linear elastic constants  $C_{11}$  vs  $C_{33}$  (left) and shear elastic constants  $C_{44}$  vs.  $C_{66}$  (right).

## Comments:

♠ Data are very scattered depending on M,A,X.

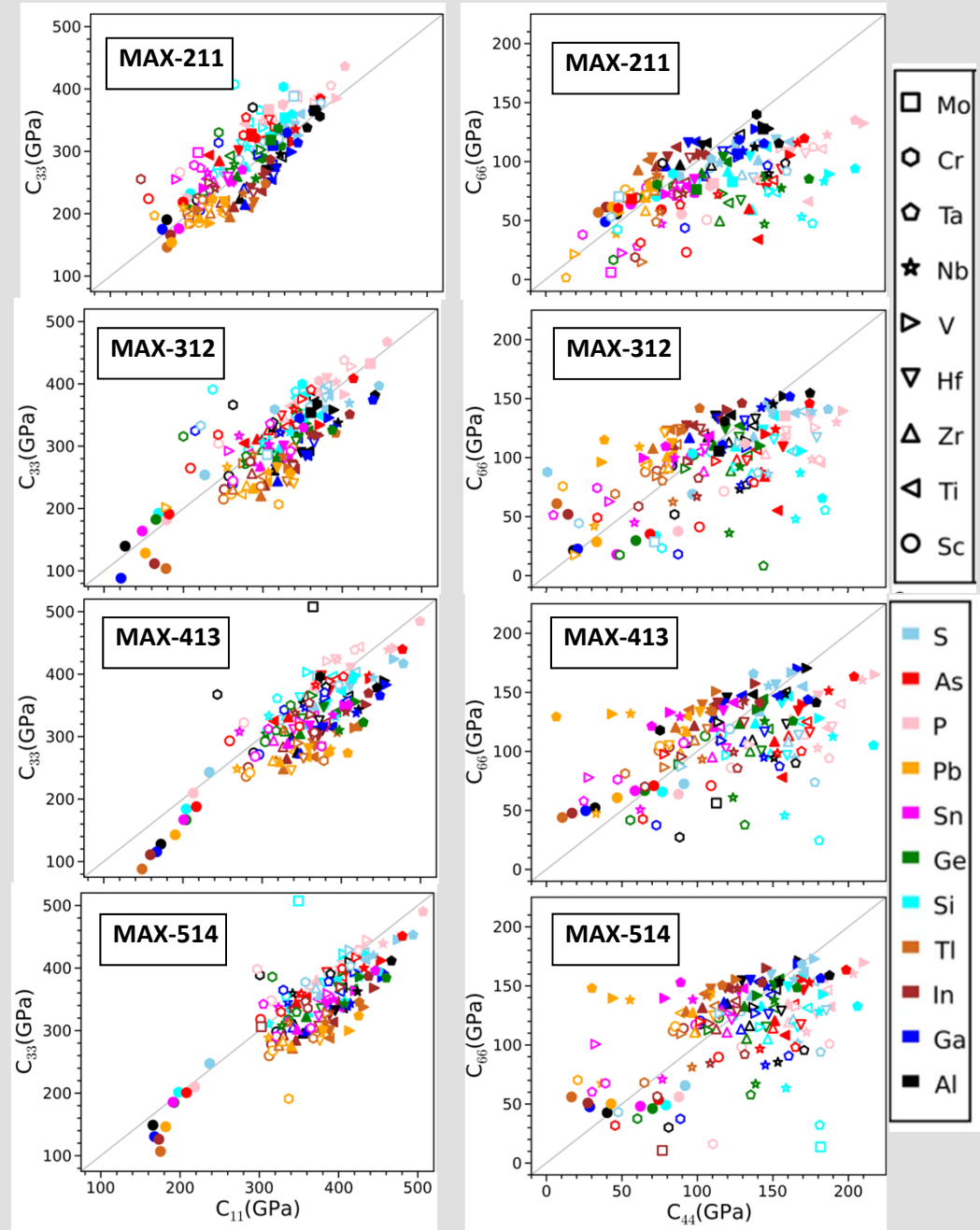
♠ Approximate linear dependence.

♠  $C_{11} \cong C_{33} \Rightarrow$  isotropic.

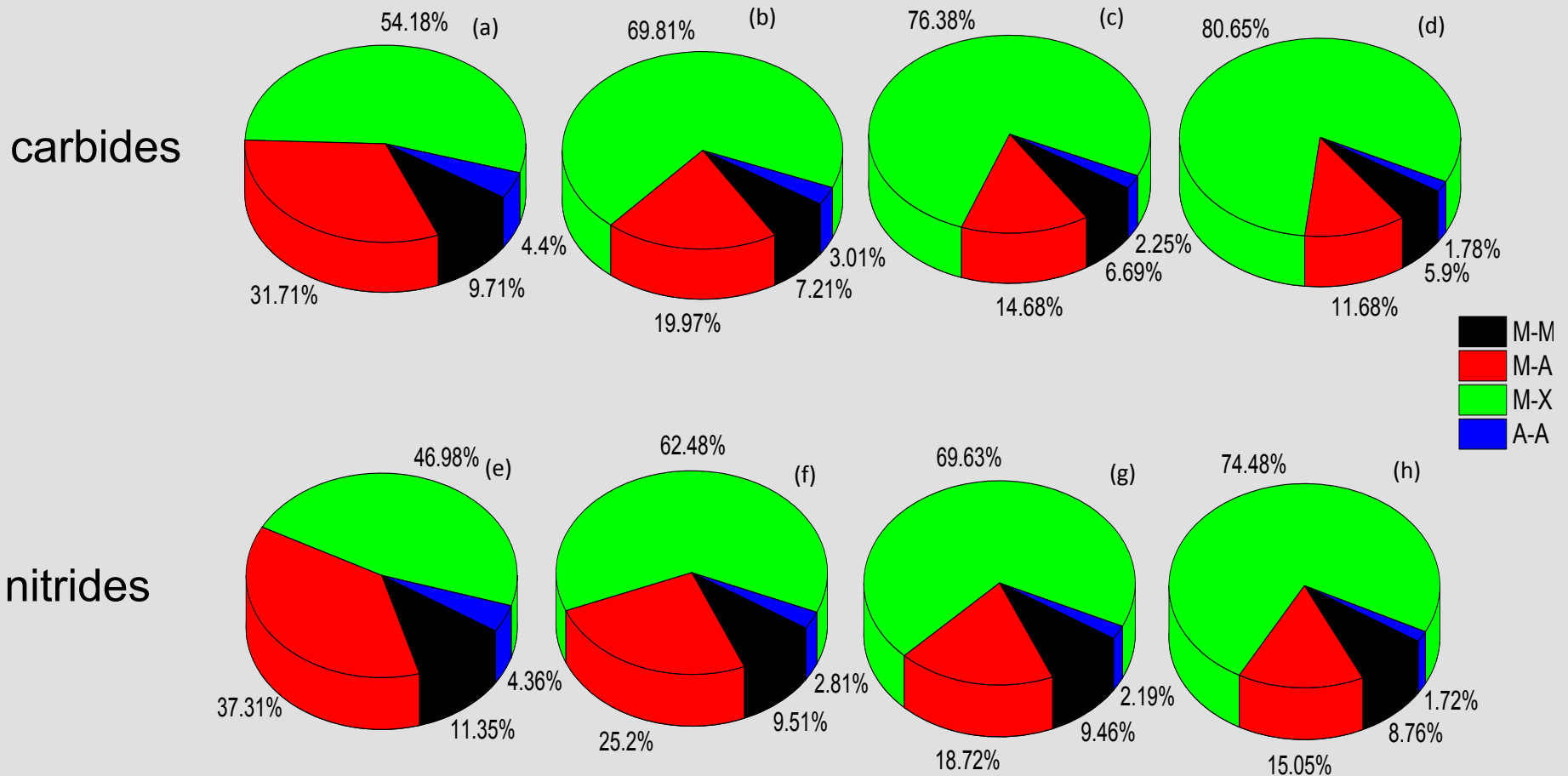
♠ trends depending on n, more linear dependence on increasing n.

♠ Marked difference in X=C and X=N.

♠ Data for  $C_{44}$  vs.  $C_{66}$  more scattered and less well defined trends.

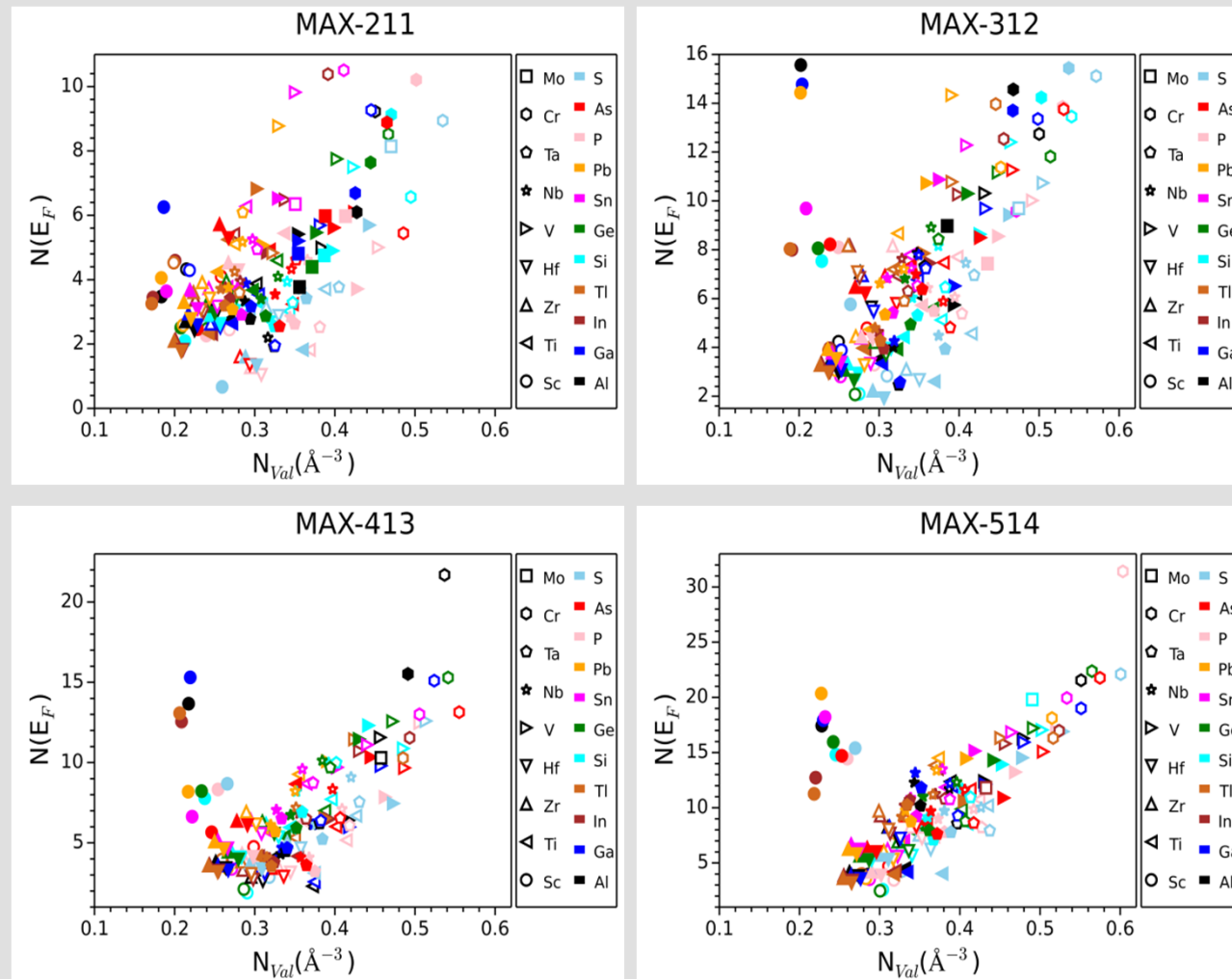


**(2) Electronic Structure Results:** Contributions from M-M, M-A, M-X, A-A pairs to the total bond order in the form of pie charts, (a) 211, (b) 312, (c) 413, (d) 514 carbides; (e) 211, (f) 312, (g) 413, (h) 514 nitrides.



- ♠ Relative distribution: M-X > M-A > M-M > A-A.
- ♠ Distribution different between carbides and nitrides.
- ♠ M-X more important in Carbides; M-A more important in Nitrides.

**(2) Electronic Structure Results:** Plot of DOS at Fermi level  $N(E_F)$  against total number of valence electrons per unit volume in the crystal.



- ♠  $N(E_F)$  in metals and alloys, a single parameter for electronic structure.
- ♠ Data are scattered but have approximate linear correlation.
- ♠ **Sc**-based carbides is an exception (absences of  $d$  electrons).

### (3) Correlation between mechanical Property and electronic structure:

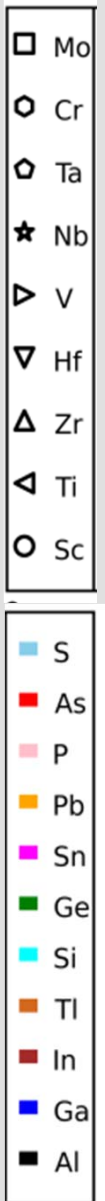
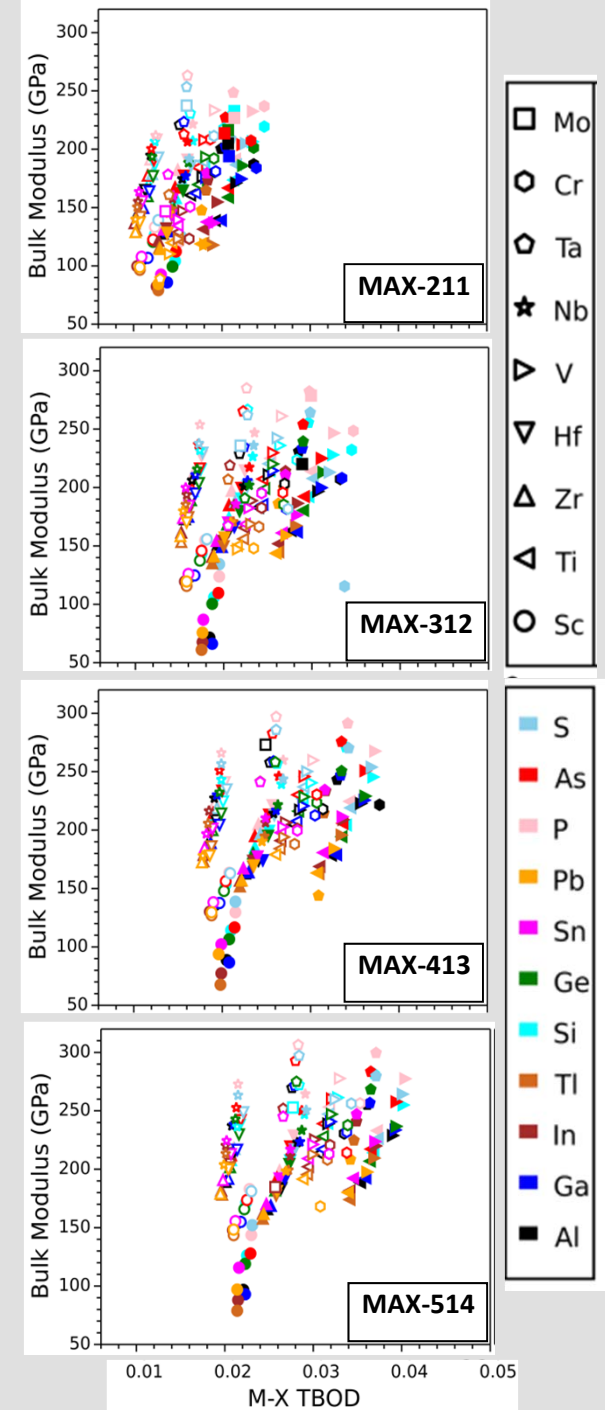
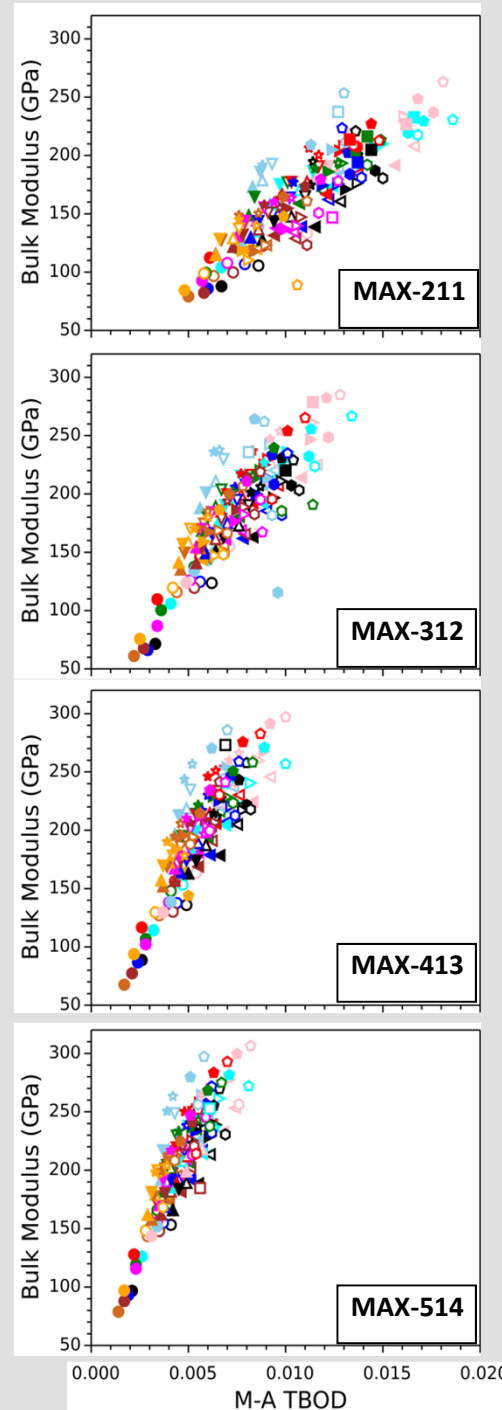
Correlation plots of bulk modulus (K) vs. M-A part of the TBOD (left) and M-X part of the TBOD (right). Other plots are not shown here.

#### Comments:

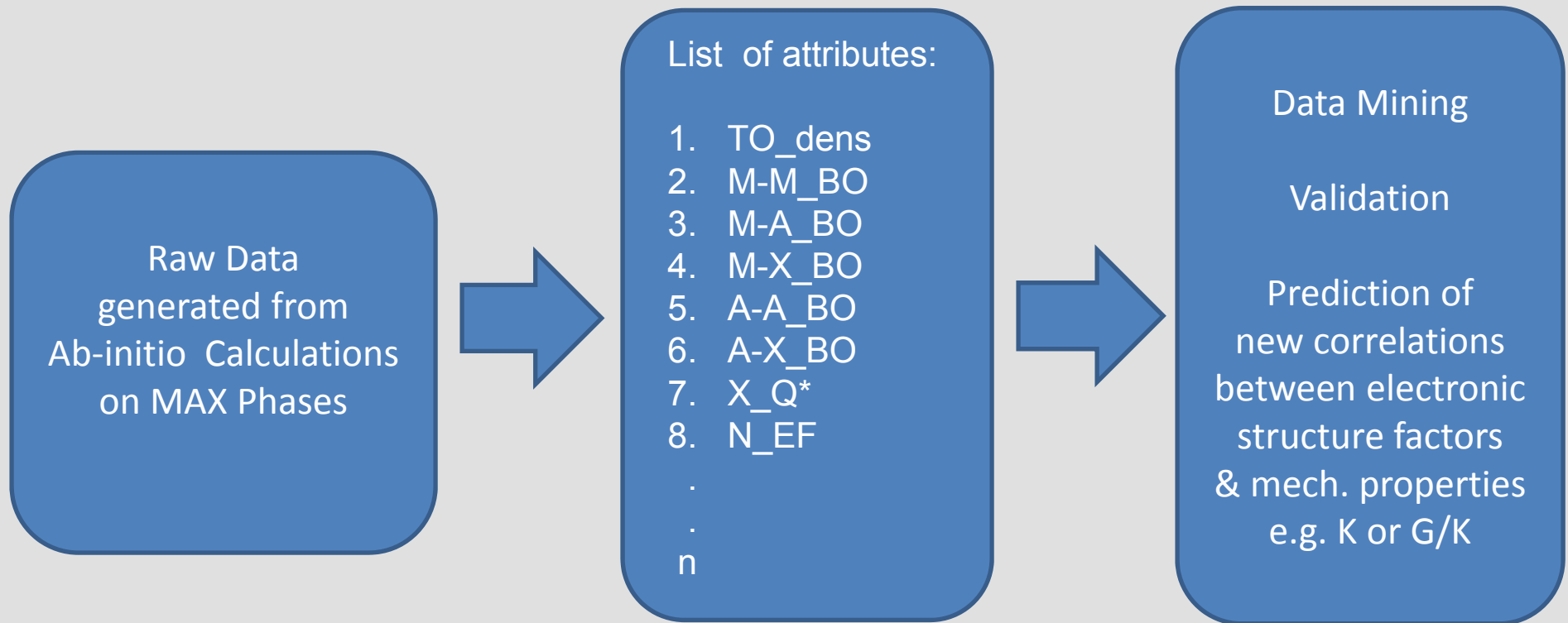
♠ K has beautiful linear correlation with M-A TBOD than M-X, but M-X has larger contribution!

♠ The slope of linear correlation increase with n.

♠ The reason is A plays a crucial role in the elastic and electronic properties of MAX phases.



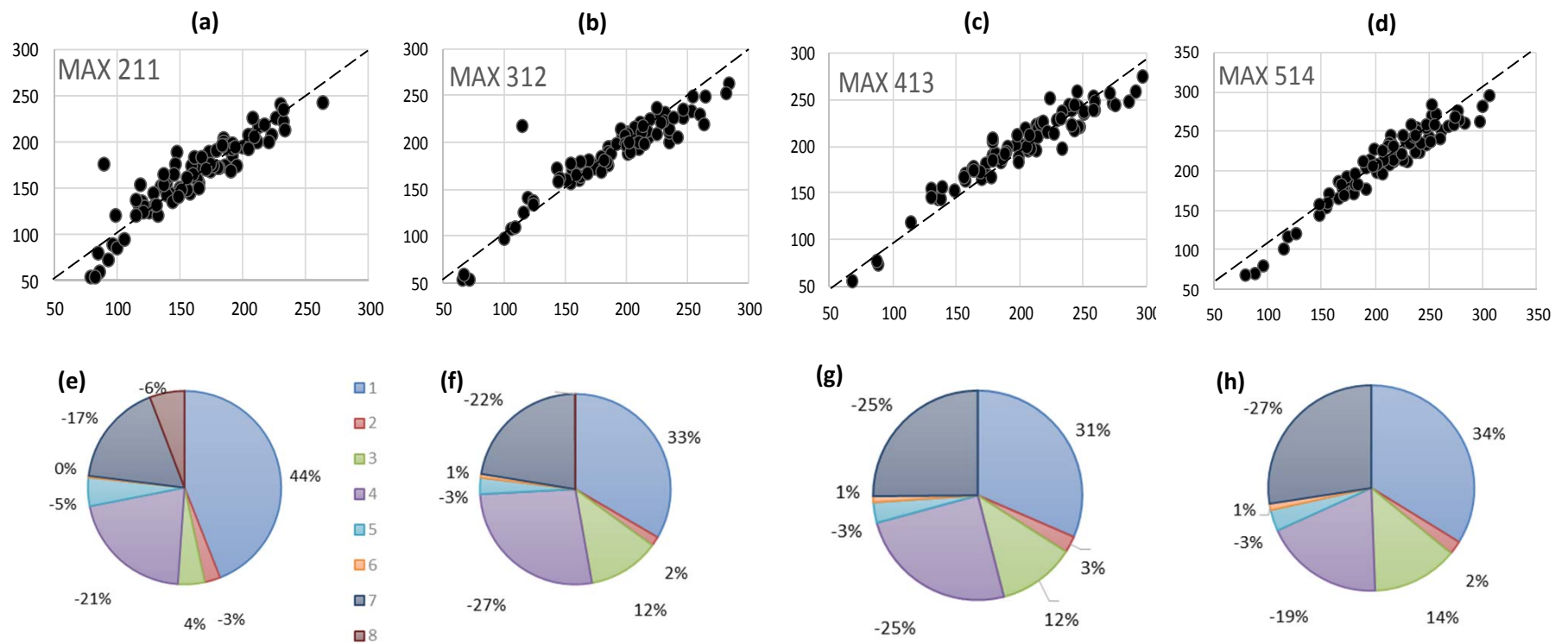
# Materials Informatics: ab-initio-data-Based Machine Learning & Data Mining



# Materials Informatics: ab-initio-data–Based Machine Learning & Data Mining

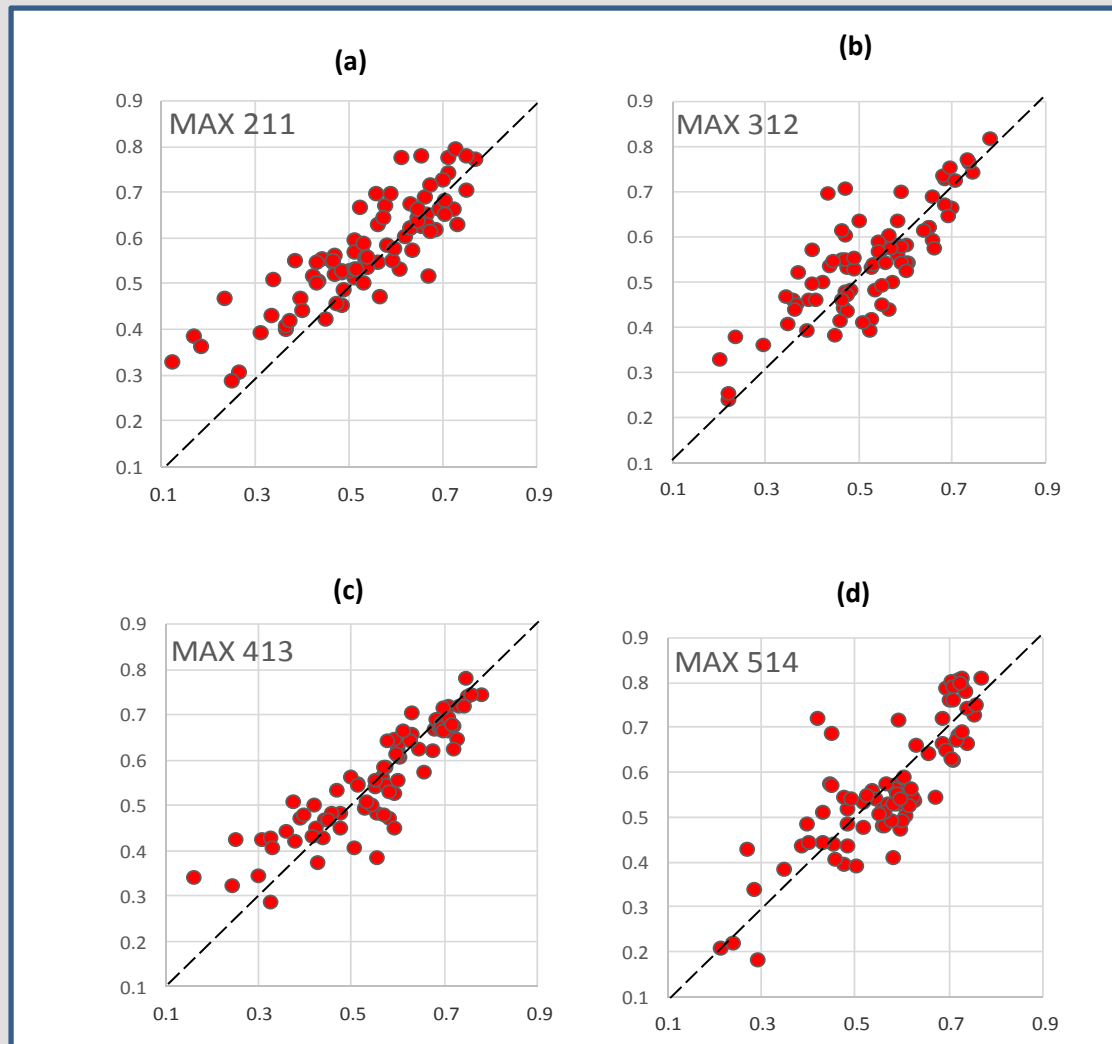
- ♠ Based on the 665 data point we have for the MAX phases to test the efficacy of the current popular data mining algorithm:
- ♠ Use 50 % of the data as the training set to predict the properties of the other 50% by comparing with those calculated using *ab initio* methods.
- ♠ Over 90 % of predictability validates the concept of **genomic approach**.





**a-d** Comparative plots of **bulk modulus** from ab-initio DFT calculations versus that from data-mining algorithm using half of randomly chosen a) 211, b) 312, c) 413 and d) 514 MAX phases,

**e-h** Pie-charts showing the average relative contributions of each electronic structure factors to the predicted bulk modulus. 1 = TOBODs, 2 = M-M\_BO, 3 = M-A\_BO, 4 = M-X\_BO, 5 = A-A\_BO, 6 = A-X\_BO, 7 = X\_Q\*, 8 = N( $E_F$ ).



Comparative plots of  $G/K$  from ab-initio DFT calculations versus that from data-mining algorithm using half of randomly chosen: a) 211, b) 312, c) 413 and d) 514 MAX phases. The correlation is still impressive ( $> 80\%$ )

## V. Summary and Conclusions

- ♠ Large data base has been constructed for **all** MAX phases. These include both the mechanical parameters and electronic structures.
- ♠ Results consistent with experiment. The screened out phases are shown to be non-existent.
- ♠ There are noticeable trends in the nature of the mechanical properties based on their positions in the Periodic Table.
- ♠ Correlations to the electronic structure and bonding and mechanical properties has been identified. (**Main goal!**)
- ♠ These data base will be extremely valuable to experimentalists who try to synthesize new MAX phases in laboratories.
- ♠ This data base is used to test the algorithms for data mining and machine learning informatics in materials research.
- ♠ Quality of the database is extremely important!

**We consider our NETL project to be highly successful for a purely computational project!**

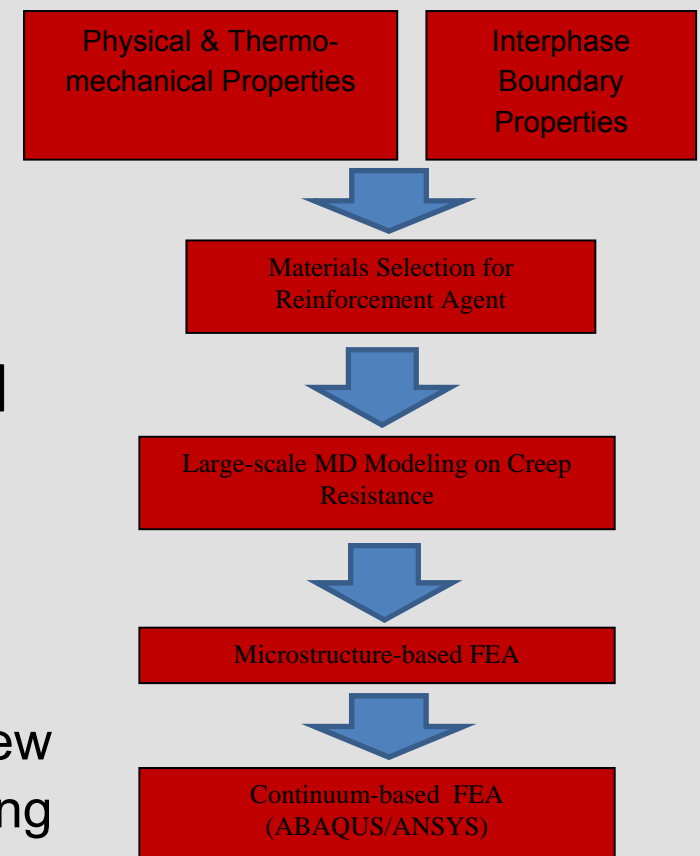
## VI. Future Work

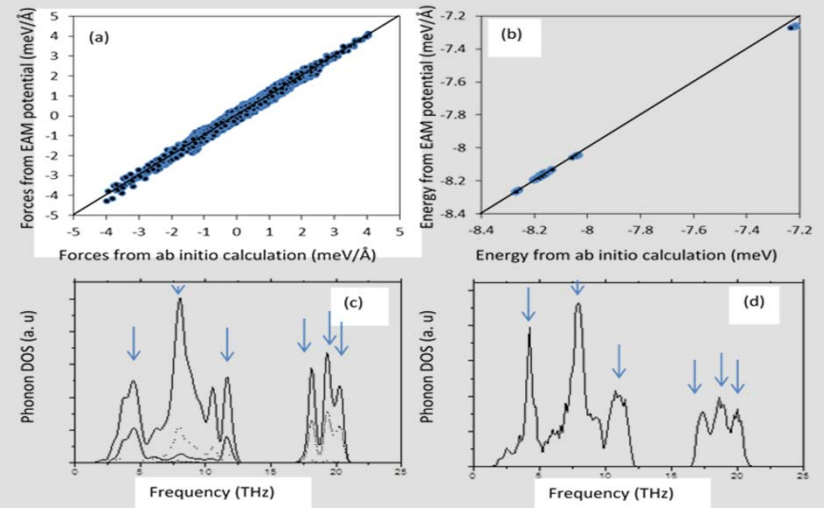
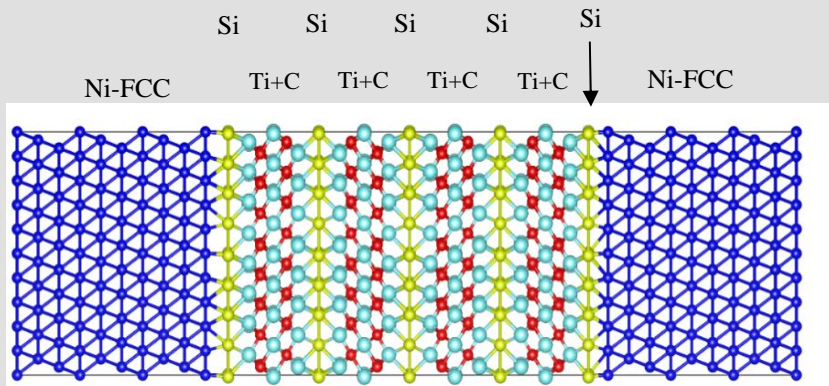
- ♠ Extend to solid solutions and composites in MAX phases.
- ♠ Extend elements **M**, **A**, **X** and to Mxenes and MAX-like phases.
- ♠ Extension to include other properties such as chemical composition, corrosion resistance, thermoconductivity, optical properties, failure behavior, high temperature properties etc.

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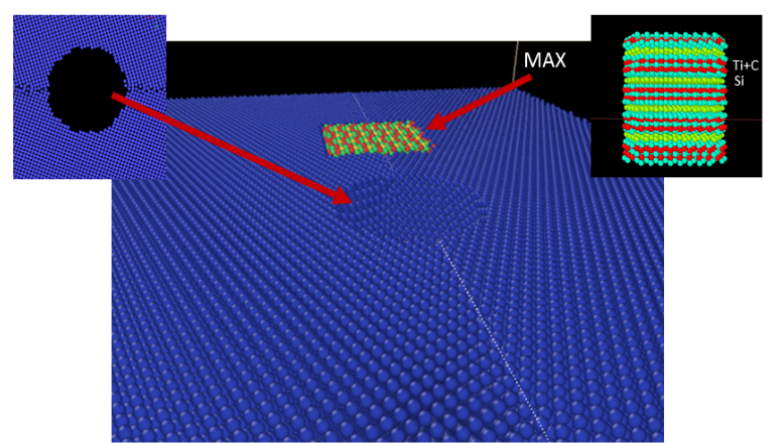
♠ We are in the process of using **genomic** approach for modeling interfaces and microstructures in Ni-based A-USC alloys to address the weldment problem in fossil energy materials by using MAX phases as strengthening agents under severe environment.

Schematics of the work flow of a new roadmap to integrate a strengthening MAX phase into A-USC alloys.

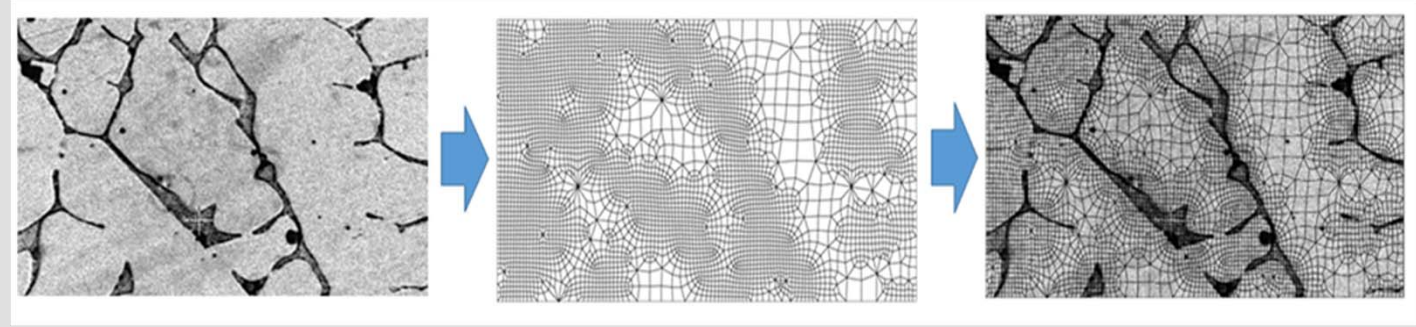




↑ Comparison **a)** Force & **b)** Total Energy. **c-d)** Phonon DOS from ab initio calculations vs. EAM potential.



← Large scale (> 1 million atom) classical MD simulation to simulate the creep resistance of MAX-reinforced HAZ.



↑ Application of atomic scale simulation to continuum model: (a) SEM micrograph of HAZ, (b) microstructure based EFM code with dense mesh, (c) FEA simulation.



# *Thank you!*

## *Acknowledgment:*

Work supported by DOE- NETL grant DE-FE00005865

Computational support from NERSC under DOE Office of Science support: DE-AC03-76SF00098



## Ab-initio-data-Based Machine Learning and Data Mining

List of coefficients for K and G/K estimates from data-mining algorithm using a linear superposition:

$$Y = C(0) + C(1)*TB\_Dens + C(2)*M-M\_TBO + C(3)*M-A\_TBO + C(4)*M-X\_TBO + C(5)*A-A\_TBO + C(6)*A-X\_TBO + C(7)*X\_Q* + C(8)*N\_E_F$$

| Y         | C(0)    | C(1)     | C(2)    | C(3)    | C(4)     | C(5)    | C(6)    | C(7)    | C(8)    | Correlation coefficient |
|-----------|---------|----------|---------|---------|----------|---------|---------|---------|---------|-------------------------|
| K(211)    | 206.839 | 5038.871 | -6.1583 | 3.2376  | -10.1989 | -28.091 | 100.743 | -107.34 | -1.2531 | 0.915                   |
| K(312)    | 187.743 | 3970.885 | 2.9706  | 11.89   | -7.2138  | -22.733 | -7.2138 | -82.193 | -0.3916 | 0.9323                  |
| K(413)    | 230.349 | 4110.439 | 4.6844  | 11.738  | -5.4867  | -21.675 | 262.329 | -126.40 | 0       | 0.9516                  |
| K(514)    | 237.707 | 4366.933 | 2.6619  | 12.386  | -4.6634  | -20.655 | 186.820 | -116.11 | -0.1278 | 0.9565                  |
| G/K (211) | 0.2209  | 8.2756   | -0.0261 | 0       | -0.0384  | 0.0928  | 0.7156  | 0.4762  | 0.2209  | 0.8629                  |
| G/K (312) | 0.1793  | 10.192   | -0.0386 | -0.0162 | -0.0054  | 0.0606  | 0.6404  | 0.49    | -0.0094 | 0.8189                  |
| G/K (413) | 0.2108  | 5.505    | -0.0566 | 0       | 0.0062   | 0.0316  | 0       | 0.43    | -0.0091 | 0.8957                  |
| G/K (514) | -0.032  | 4.9746   | -0.0268 | 0       | 0.0054   | 0.0371  | 0.7475  | 0.56    | -0.0054 | 0.8436                  |

Examples of MAX phase outliers with either Sc-based or with a relatively low G/K and potentially thermodynamically stable i.e with a negative  $\sum\Delta H$  or with  $\sum\Delta H \leq + 0.0253$  eV

| MAX                              | G/K   | CHEMICAL EQUILIBRIA   | $\sum\Delta H$ (eV/atom) |
|----------------------------------|-------|---|--------------------------|
| Sc <sub>3</sub> TiN <sub>2</sub> | 0.685 | Ti + Sc + 2 ScN = Sc <sub>3</sub> TiN <sub>2</sub>                    | - 0.0638                 |
| Ta <sub>2</sub> GeC              | 0.671 | Ta <sub>2</sub> C + TaC + TaGe <sub>2</sub> = 2 Ta <sub>2</sub> GeC   | -0.03430                 |
| Ta <sub>3</sub> GeC <sub>2</sub> | 0.700 | Ta <sub>2</sub> C + 3 TaC + TaGe <sub>2</sub> = 2 Ta <sub>3</sub> GeC | -0.04800                 |
| Ti <sub>2</sub> AsC              | 0.430 | TiC + TiAs = Ti <sub>2</sub> AsC                                      | +0.01854                 |
| Mo <sub>2</sub> GeC              | 0.375 | 3 Mo <sub>2</sub> C + 2 MoGe <sub>2</sub> + C = 4 Mo <sub>2</sub> GeC | +0.02528                 |



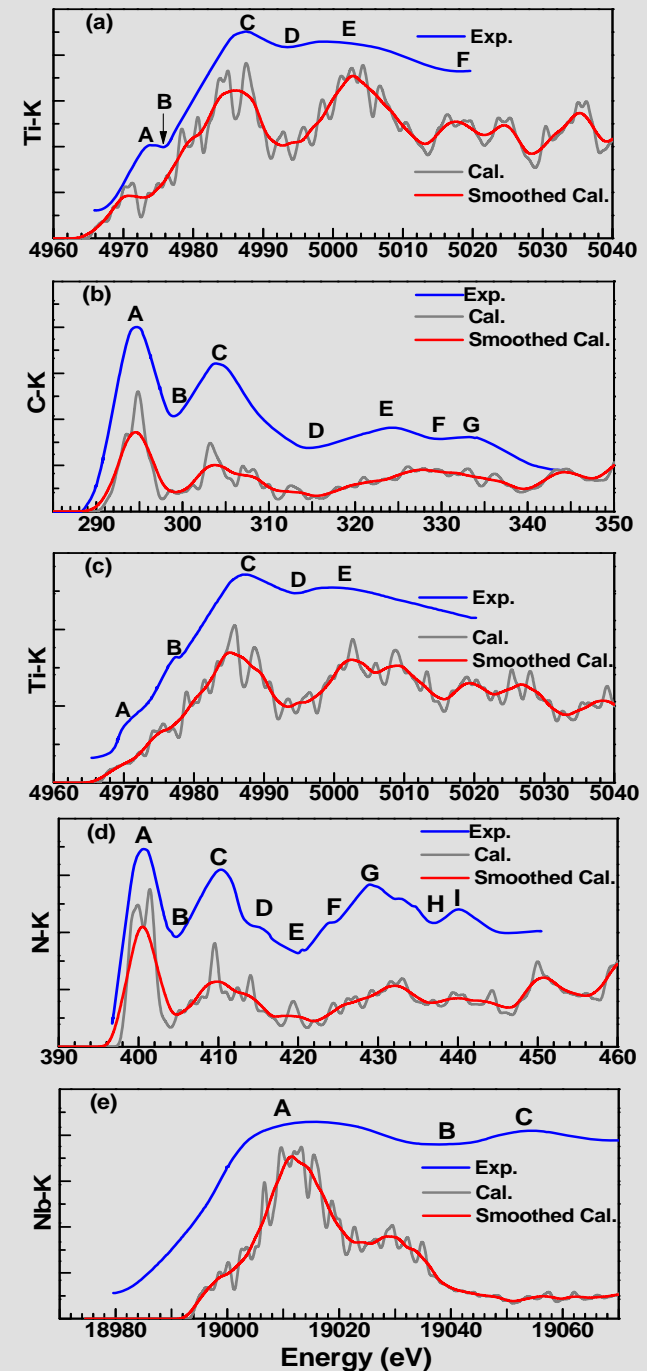
# ELNES Spectral Calculation of MAX phases

♠ The spectra of Ti-K edges in  $Ti_2AlC$  and  $Ti_2AlN$ , C-K edge in  $Ti_2AlC$ , N-K edge in  $Ti_2AlN$ , and Nb-K edge in  $Nb_2AlC$  are calculated and found to be in good agreement with reported experimental measurements.

♠ More details can be found in:

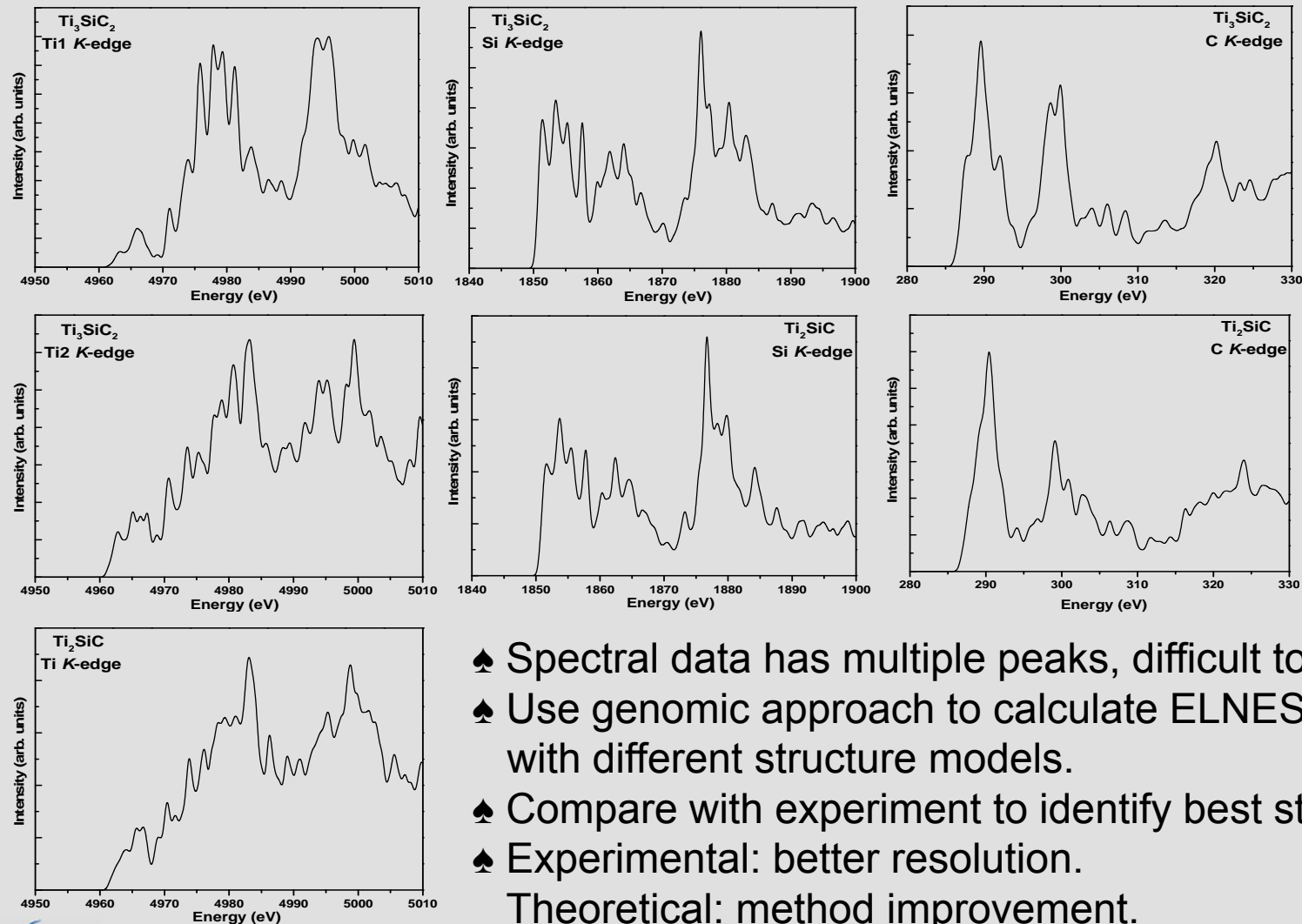
*Liaoyuan Wang, Paul Rulis, W. Y. Ching, "Calculation of core-level excitation in some MAX phase compounds", J. Appl. Phys. 114, 023708 (2013).*

♠ First time OLCAO-supercell method applied to metallic systems. Core-hole effect less important than in insulators.



# ELNES Spectral Calculation of MAX phases

♠ ELNES spectra for  $\text{Ti}_2\text{SiC}$  and  $\text{Ti}_3\text{SiC}_2$  Spectra (unpublished!)



- ♠ Spectral data has multiple peaks, difficult to interpret.
- ♠ Use genomic approach to calculate ELNES spectra with different structure models.
- ♠ Compare with experiment to identify best structure.
- ♠ Experimental: better resolution.  
Theoretical: method improvement.